

# Accuracy Assessment of Some Potential GNSS Positioning Techniques for Ellipsoidally Referenced Hydrographic Surveys



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한국수로학회

# :: OUTLINE ::

## I INTRODUCTION

## II GNSS DATA AND METHODOLOGY

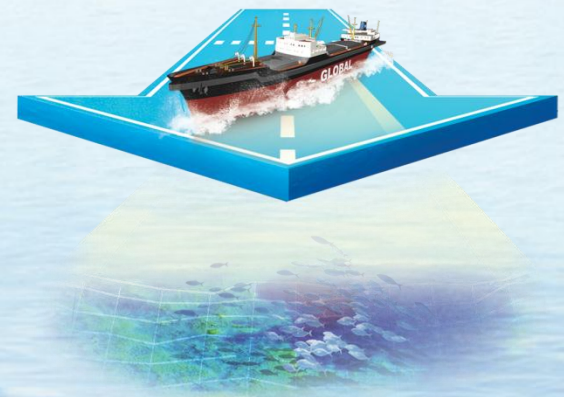
## III RESULTS AND DISCUSSION

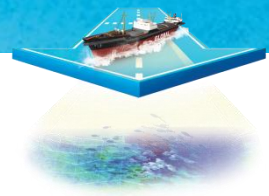
## III CONCLUDING REMARKS





I

# INTRODUCTION





# VERTICAL DATUM (HEIGHT SYSTEM)

-  A one-dimensional coordinate system
-  Used to define the metric distance of some point **from reference surface along a well-defined path** (i.e., the height of the point)

## COMPONENT



**Datum Surface + Path that the distance is measured over**

## CLASSIFICATION

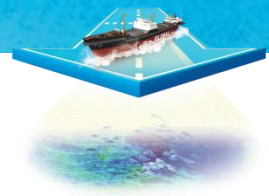
**Not related to** Gravity using straight-line path

**Related to** Gravity using curved path (e.g., plumbline)

## WHICH CLASS OF THE SYSTEM IS NATURAL AND PHYSICALLY MEANINGFUL?

-  Water **must** flow **downhill** from a higher to a lower height
-  The Earth's gravitational force governs water flow





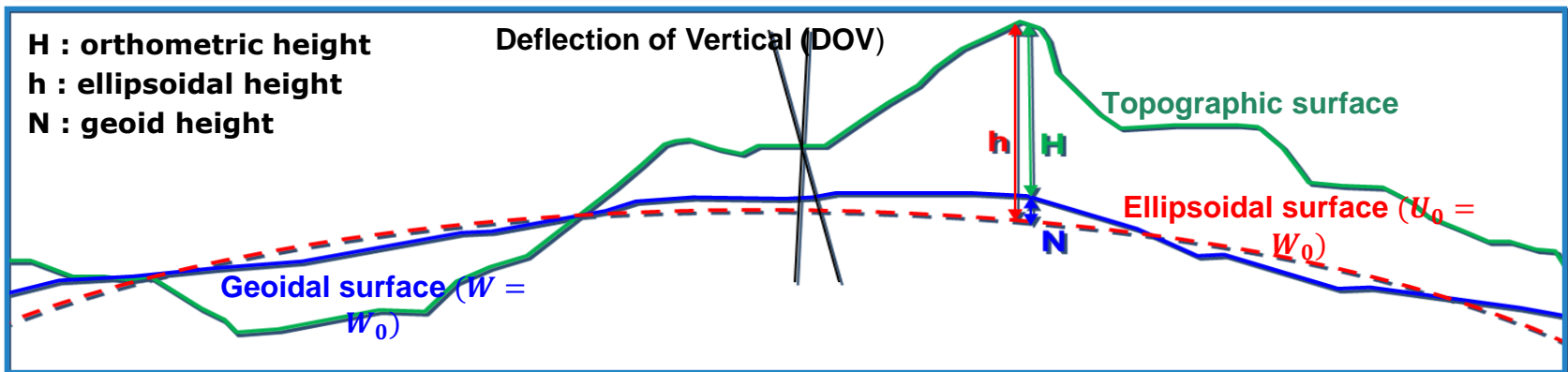
# CATEGORY OF VERTICAL DATUM (1/2)

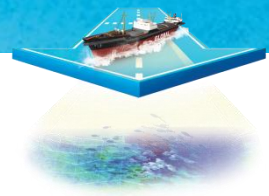
## Geodetic Vertical Datum

- ☐ Geoid is the reference surface of the geodetic datum from a theoretical standpoint.
- ☐ Equipotential surface of the Earth's gravity field which best fits (global) mean sea level in a least squares sense.
- ☐ Topographic data are often referenced to a local datum, such as Local MSL.

## Reference Ellipsoid

- ☐ Simple mathematical surface of the Earth which closely approximates the geoid.
- ☐ GNSS heights are determined relative to this surface.
- ☐ **Orthometric Height (H) = Ellipsoidal Height (h) – Geoidal Height (N)**





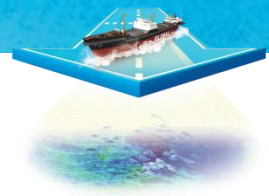
# CATEGORY OF VERTICAL DATUM (2/2)

## Chart Datum (CD)

- ☐ Used on nautical charts to reference water depths.
- ☐ Bathymetric data displayed on charts is reference to a low water tidal vertical datum (e.g., Lowest Astronomical Tide – LAT).
- ☐ Chart datums are only fully valid at the location where the tides are observed.
- ☐ Challenge in traditional hydrography is establishing relationship between the instantaneous water surface (IWS) and CD away from gauge locations.
- ☐ Uncertainty in the relationship between IWS and CD at the survey site is a significant component of the overall depth uncertainty.

- MLW      Mean Low Water
- MLLWLT      Mean Lower Low Water Large Tide
- MLLW      Mean Lower Low Water
- LNT      Lowest Normal Tide
- LLWLT      Lower Low Water Large Tide
- LAT      Lowest Astronomic Tide (atmospheric & oceanographic effects minimized)





# ELLIPSOIDALLY REFERENCED SURVEY

ONE OF THE MOST SIGNIFICANT ISSUES IN HYDROGRAPHY TODAY IS TO USE **THE ELLIPSOID AS THE REFERENCE FOR MEASURING WATER DEPTH.**

- ❑ Hydrographic survey has traditionally been performed for establishing nautical charts for safety of navigation, **but has now a vital role in costal zone management.**
- ❑ Costal zone encompasses a wide belt along the shoreline including the land and sea.
- ❑ **Integration of hydrographic and topographic data is essential for the analysis of coastal processes and sound management decision.**
- ❑ **GPS derived-heights on land and seas can be readily related to one another by GEOID, HYDRODYNAMIC & TSS MODELS.**
- ❑ The ellipsoid is convenient surface for field surveying, but **it has only geometrical meaning.**
- ❑ **The ellipsoidally referenced spatial information should be transformed to geodetic or chart datum.**

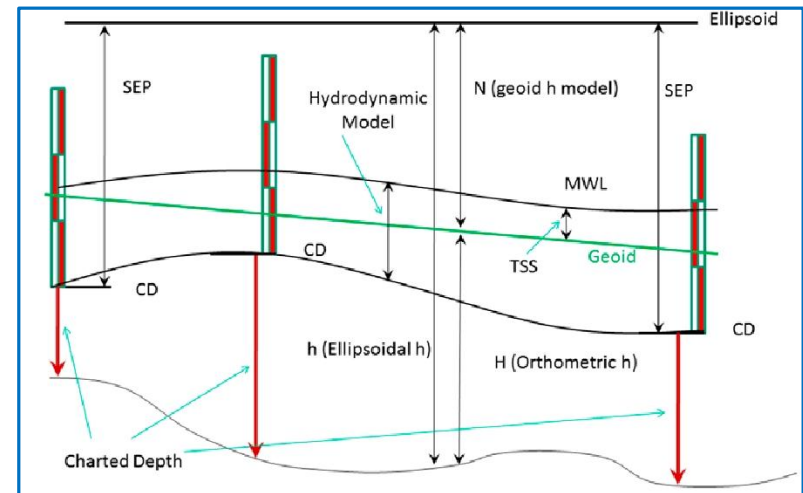
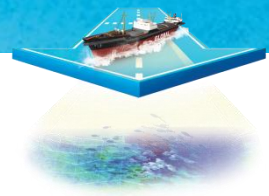





FIG (2014) Ellipsoidally reference surveying for hydrography, Publication No. 62, 62pp.



# TECHNICAL ISSUES IN ERS

- I Data acquisition of high accuracy of GNSS
- II GNSS data processing scheme and its accuracy (uncertainty)
- III Vertical separation model (SEP) development and application
- IV Quality control of vertical offset, GNSS, motion, SEP.
- V Uncertainty associated with offset, GNSS, motion and SEP
- VI Data archive reference

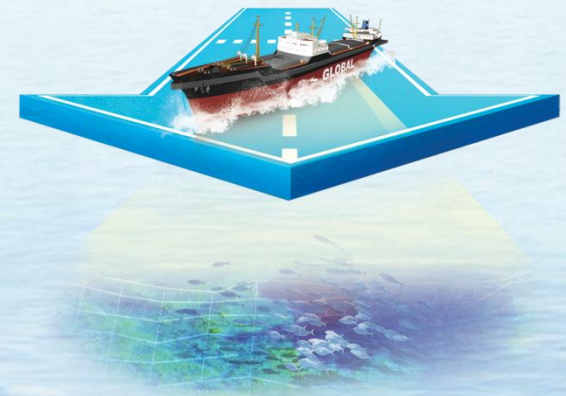
FIG (2014) Ellipsoidally reference surveying for hydrography, Publication No. 62, 62pp.

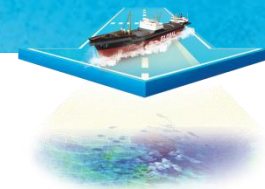
-  This presentation focuses on the first and second issue.
-  GNSS data collected in **static and kinematic mode** has processed by two **different strategies and software**.
-  **Accuracy of GNSS-derived ellipsoidal height** is mainly discussed.



## II

# GNSS DATA & METHODOLOGY





# GNSS MEASUREMENT EQUATIONS

## 1 Pseudo-Range (PR)

$$R_i^s = \rho_i^s + \boxed{d\rho_i^s + c(dt^s - dT_i)} + di_i^s + dr_i^s + dm_{i,R}^s + \varepsilon_{i,R}^s$$

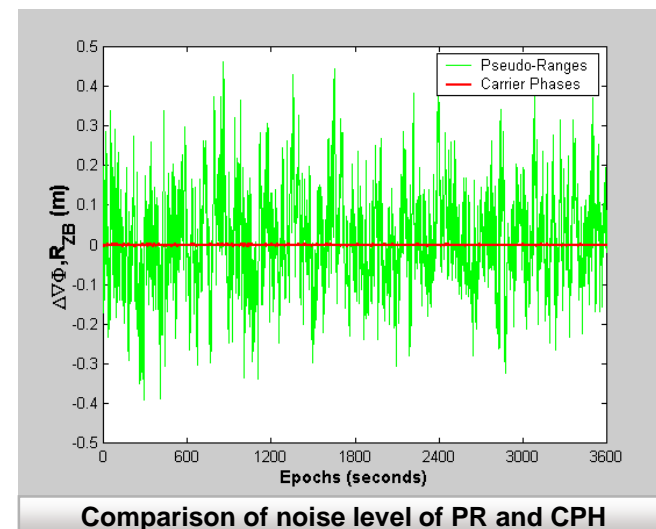
## 2 Carrier-Phase (CPH)

$$\lambda_G \cdot \phi_i^s = \rho_i^s + \boxed{d\rho_i^s + c(dt^s - dT_i)} + \lambda_G \cdot N_i^s \boxed{-di_i^s + dr_i^s} + dm_{i,\phi}^s + \varepsilon_{i,\phi}^s$$

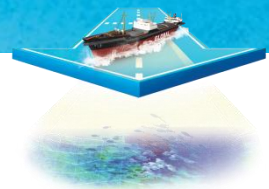
Data processing schemes depend upon

- ☐ Type of measurements used for estimation of coordinates (PR Vs. CPH);
- ☐ Method how errors boxed in the equations are handled (Point Vs. Relative).

To maximize positioning accuracy, CPH should be used for estimation process.





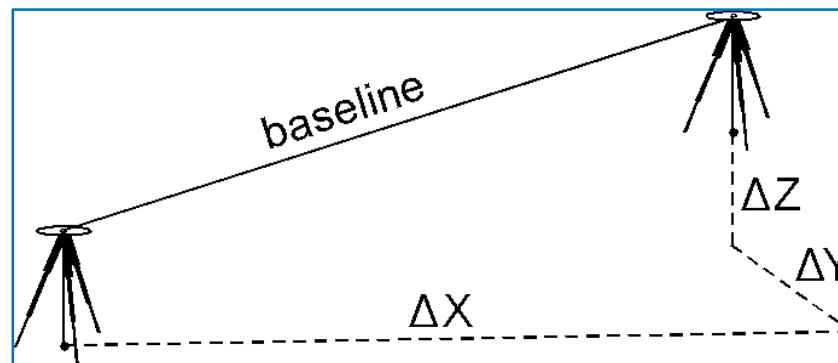


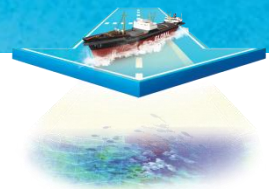
# PRECISE RELATIVE POSITIONING (PPK)

With two GNSS receivers tracking the same satellite signal at the same epoch, **differencing technique** is applied for the measurements to:

- 1 Eliminate satellite clock bias (and SA when it was on).
- 2 Reduce the effect of satellite ephemeris bias.\*
- 3 Reduce the effect of reference station coordinate bias.\*
- 4 Reduce the effect of ionospheric bias.\*
- 5 Reduce the effect of tropospheric bias.\*

**\*Degree of reduction depends on baseline length ...**





# PRECISE RELATIVE POSITIONING (PPK)

DOUBLE-DIFFERENCING (DD) TECHNIQUE IS COMMONLY USED FOR CPH PROCESSING

## 1 Short Baseline (< 20km)



$$\lambda \cdot \Delta \nabla \phi_{ij}^{st} = \Delta \nabla \rho_{ij}^{st} + \lambda \cdot \Delta \nabla N_{ij}^{st} + \Delta \nabla \varepsilon_{ij,\phi}^{st}$$

## 2 Medium-Baseline (20km < 1,000km)

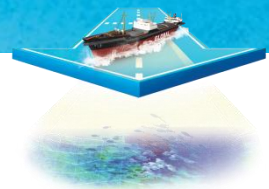
$$\lambda \cdot \Delta \nabla \phi_{ij}^{st} = \Delta \nabla \rho_{ij}^{st} + \lambda \cdot \Delta \nabla N_{ij}^{st} \boxed{- \Delta \nabla di_{ij}^{st} + \Delta \nabla dr_{ij}^{st}} + \Delta \nabla \varepsilon_{ij,\phi}^{st}$$

For 'high productivity' techniques **reliable ambiguity estimation & resolution** is crucial.

**Residual ionosphere & troposphere** biases are fundamental limit to GPS accuracy.

-  Precise satellite ephemeris should be used.
-  Residual ionosphere & troposphere biases should be estimated together with coordinates using a filter and/or smoother.








# PRECISE POINT POSITIONING (PPP)

Precise Point Positioning (PPP) refer to

- ❑ **Centimeter-level** positioning accuracy of **a single static receiver** using a long observation series,
- ❑ **Sub-decimeter-level** accuracy of **a single moving receiver** using **ionospheric-free** pseudo-range and carrier phase measurements.

1 All known error correction must be applied to PR and CPH.

-  **Precise satellite ephemeris (e.g., IGS, CODE)**
-  **Satellite clock correction (e.g., IGS, CDE)**
-  **Tropospheric delay model (e.g., Hopfield, Saastamoinen model)**

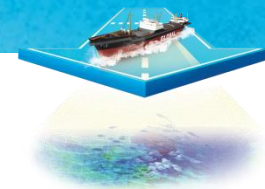
2 Forming ionospheric-free combination to eliminate ionospheric effects

$$R_{i,free}^S = \rho_i^S - c \cdot dt_i + dr_i^S + \varepsilon_{R,i}^S$$

$$\lambda \phi_{i,free}^S = \rho_i^S - c \cdot dt_i + \lambda N_i^S + dr_i^S + \varepsilon_{\phi,i}^S$$

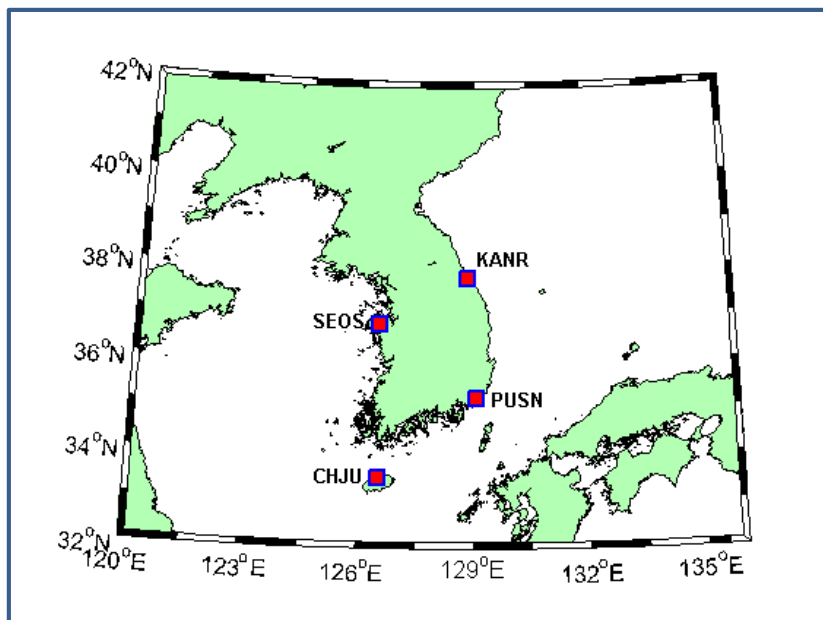
The receiver clock bias and the residual troposphere are estimated together with the receiver coordinates in the processing.

# GNSS DATA



## Static Case

- Five CORS stations in Korea
- 24 hours GPS data
- Over 250km of Baseline length



## Kinematic Cases

### Turn-table Test

- Sokkia GRS2600 (dual-frequency)
- 1Hz sampling rate
- 70 min. including 10 min. static session

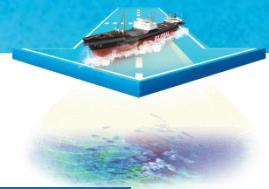


### Survey Vessel Test

- Three of Sokkia GRX1 (dual-frequency)
- 1Hz sampling rate for 2 hours
- Two hours kinematic session



Precise satellite orbit and clock (5 sec. sampling) were included in GNSS data processing.



# GNSS SOFTWARE & PROCESSING

## Software#1 (WS-1)

- An open source program package for GNSS positioning
- Standard and precise positioning algorithms with **GPS, GLONASS, SBAS, QZSS**
- Positioning mode for **real-time and post-processing: Single, SBAS, DGPS, RTK, PPP**
- Support many formats/protocols & receivers

## Software#2 (WS-2)

- Commercial post-processing software by Novatel
- Highly configurable processing engine that allows for **the best possible static or kinematic accuracy.**
- Differential and PPP processing
- Support multiple reference station
- Support for GPS L1/L2/L2C, GLONASS, BeiDou

Evaluation of achievable accuracy of ellipsoidal height estimated by medium-range PPK and PPP

### Medium-Range Baseline PPK

- ✓ CODE precise satellite orbit
- ✓ Estimation of Iono. & trop.
- ✓ Ambiguity float solutions
- ✓ Combination of forward & backward processing

### Short Baseline PPK

- ✓ Generation of reference for accuracy evaluation
- ✓ Ambiguity fixed solutions
- ✓ Usage of the nearest base station (e.g., shorter than 3km)

### PPP - Kinematic

- ✓ CODE precise satellite orbit
- ✓ CODE 5 sec. satellite clock
- ✓ Ambiguity float solutions
- ✓ Combination of forward & backward processing

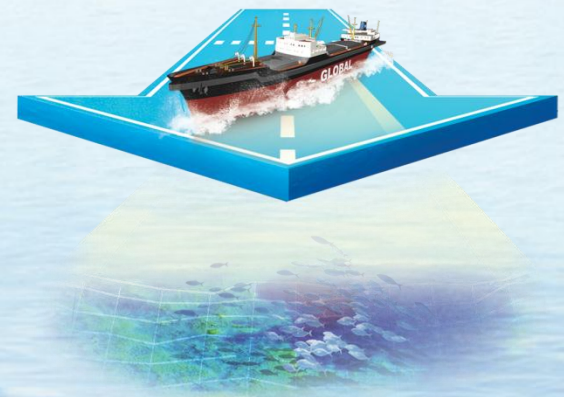
Comparison!

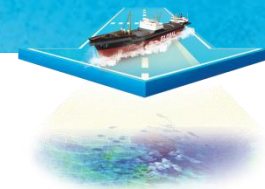
Comparison!



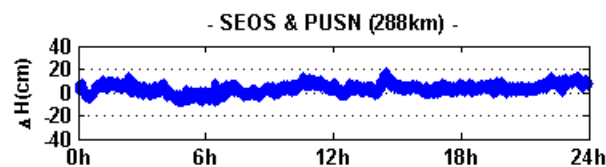
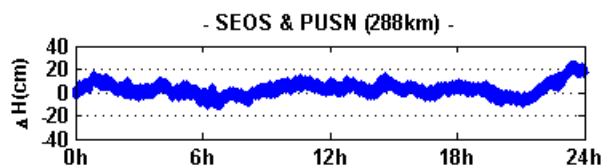
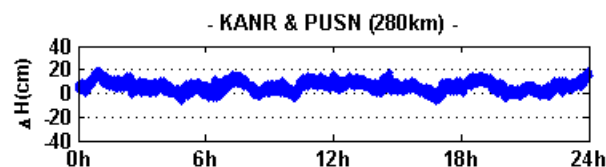
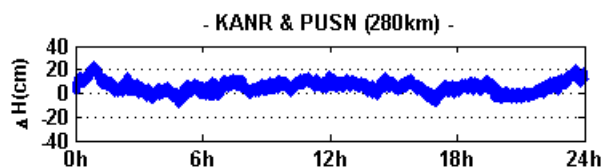
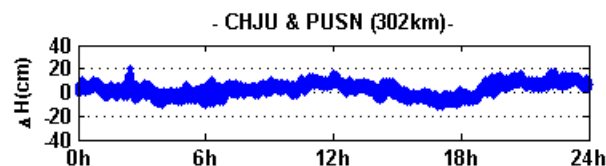
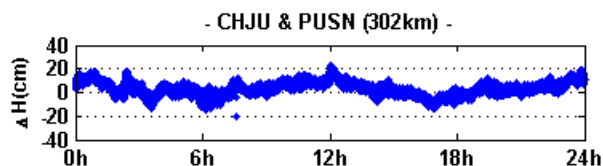
### III

## RESULTS AND DISCUSSION





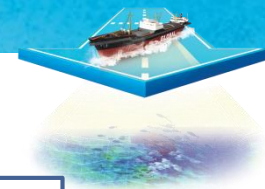
# STATIC TEST - PPK



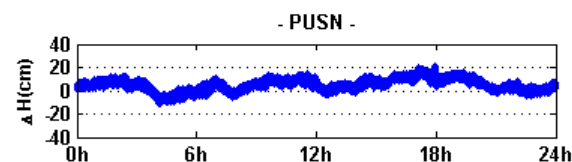
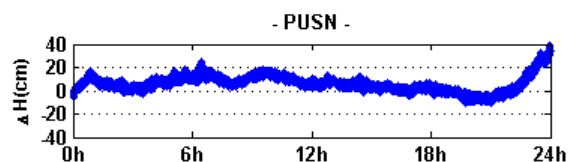
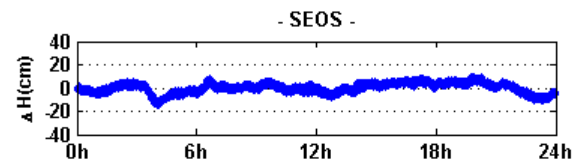
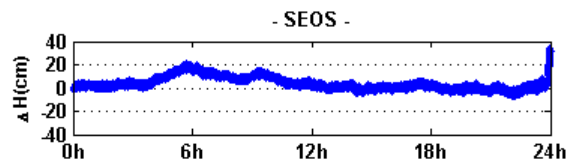
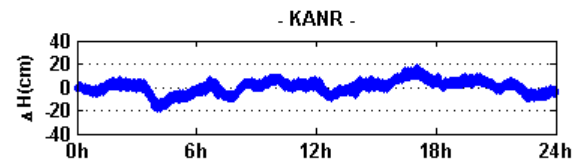
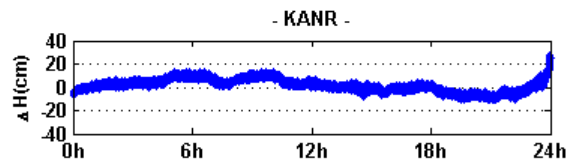
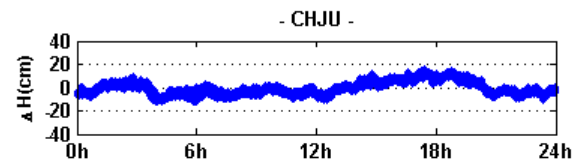
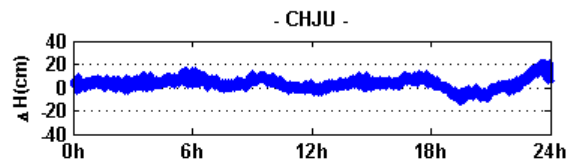
SW-1

- SW-2 -

- ✓ Three baseline solutions were generated by each software.
- ✓ Time-series of coordinate differences between PPK-derived and published height.
- ✓ Graphs in left column: solutions from SW-1
- ✓ Graphs in right column: solutions from SW-2



# STATIC TEST - PPP



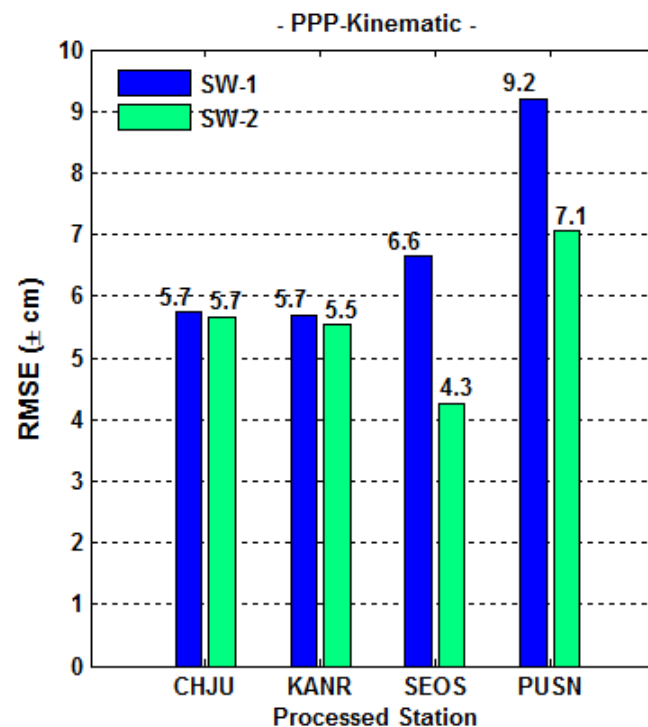
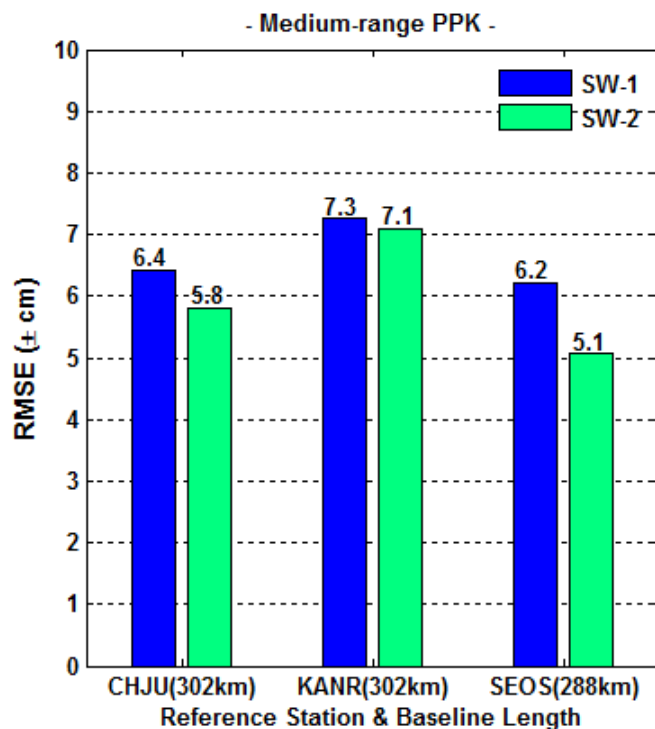
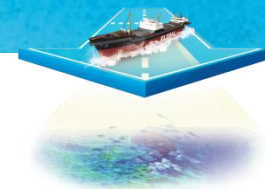
- SW-1 -

- SW-2 -

- ✓ Solutions were generated with respect to each station.
- ✓ Time-series of coordinate differences between PPP-derived and published height.

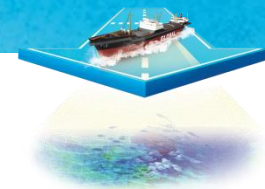


# STATIC TEST - RMSE

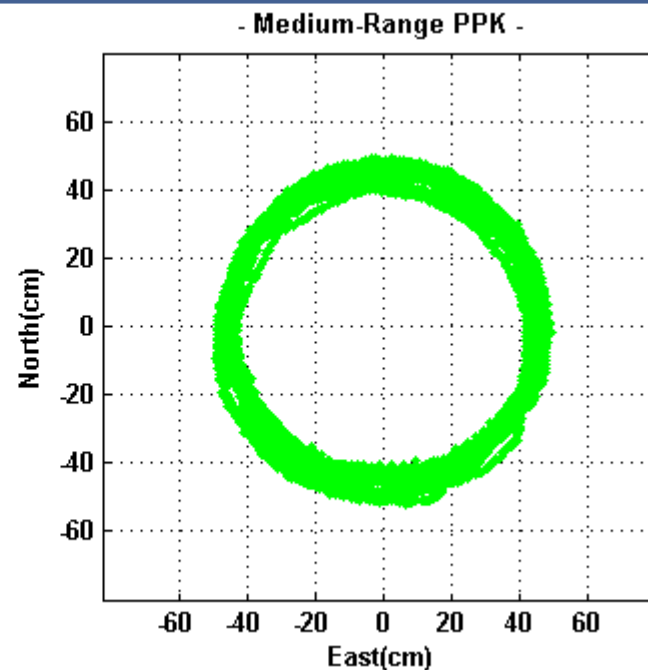
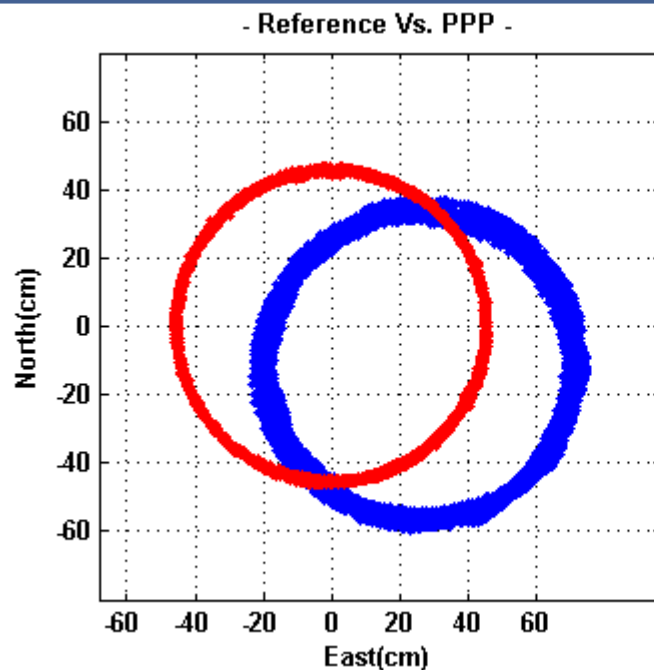


- ✓ Accuracy of PPK and PPP is almost equivalent (PPK:  $\pm 5 - \pm 7$ cm, PPP:  $\pm 4 - 7$ cm except for PPP at PUSN).
- ✓ Solutions from SW-2 are slightly more accurate than those of SW-1.

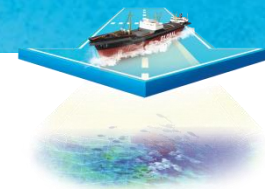
# TURN TABLE TEST - TRACE



Example of SW-2 Results

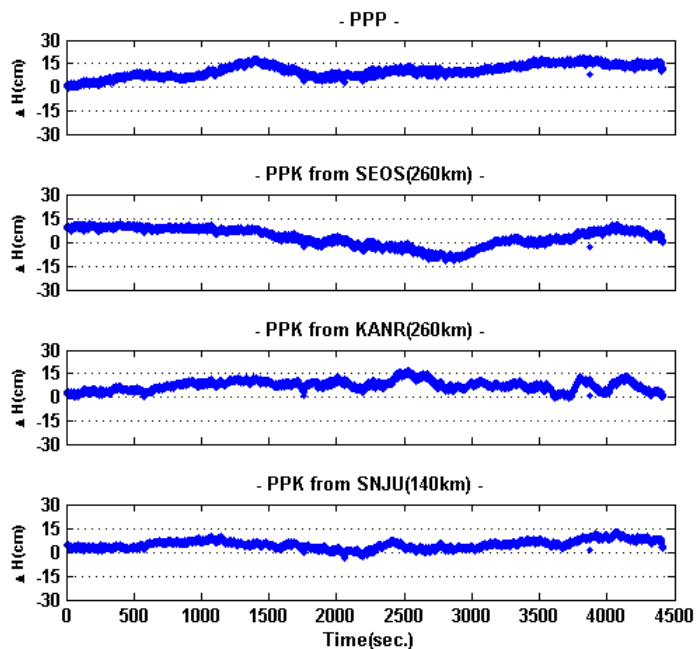


- Example of results given by SW-1 solutions
- PPK solution is obtained from baseline processing of SEOS & Turn Table (260km).
- Bias between reference and PPP is caused by different epoch of solution (i.e., KGD2002 to which the published coordinates is referenced is aligned to epoch 2002.0).

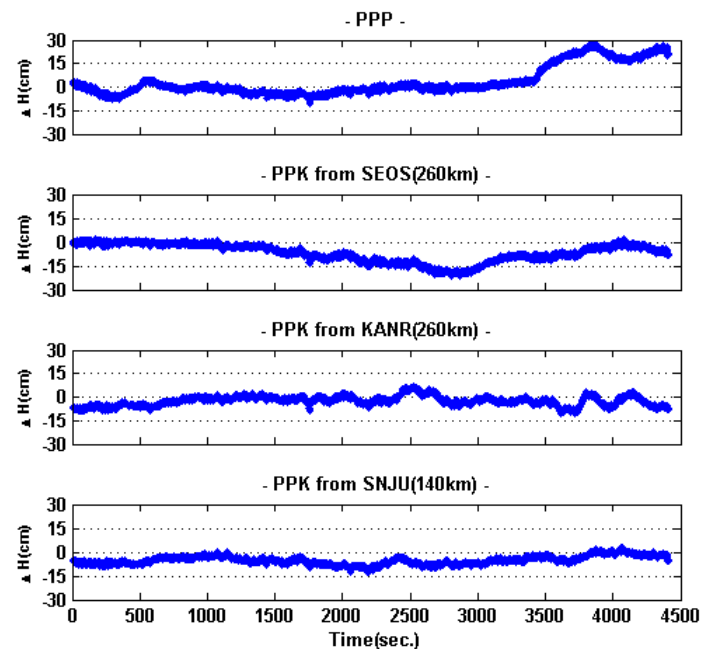


# TURN TABLE TEST – HEIGHT

SW-2: PPP Vs. PPK



SW-2: PPP Vs. PPK



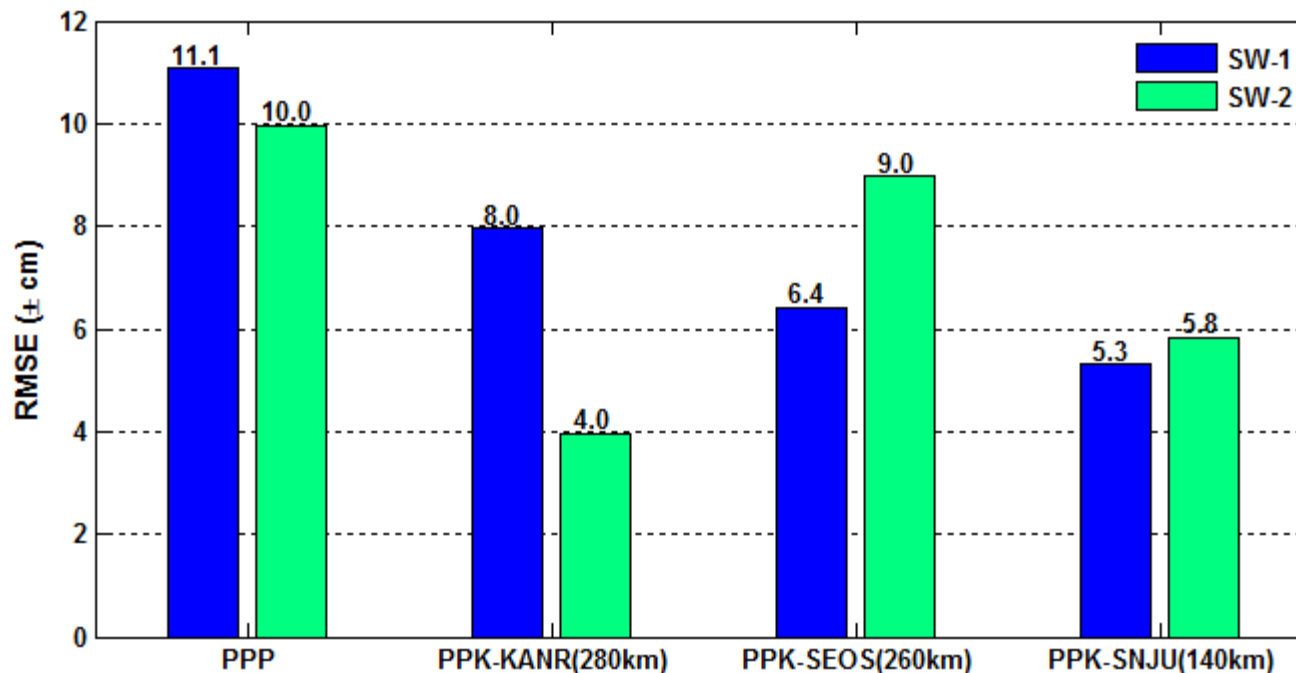
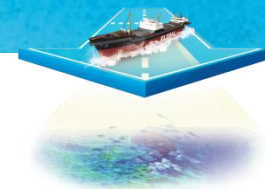
Comparing solutions given by two S/W, variation pattern is similar, but different level of bias is observed.



It seems to be caused by different modeling schemes of ionosphere and troposphere have been implemented in the software.

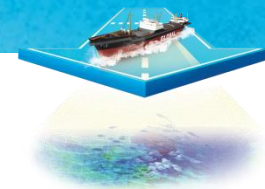


# TURN TABLE TEST – RMSE



- PPK solutions are slightly more accurate than that of PPP.
- Accuracy of PPP is around  $\pm 10$ cm while that of PPK is better than  $\pm 10$  cm
- Accuracy of PPK-KANR from SW-2 is superior to that of SW-1, but in other two cases SW-1 is a little bit better.
- Note that filter initialization is required for few tens of minutes.

# SURVEY VESSEL TEST

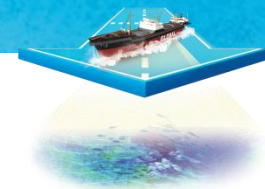


## ● Trajectory and location of reference stations

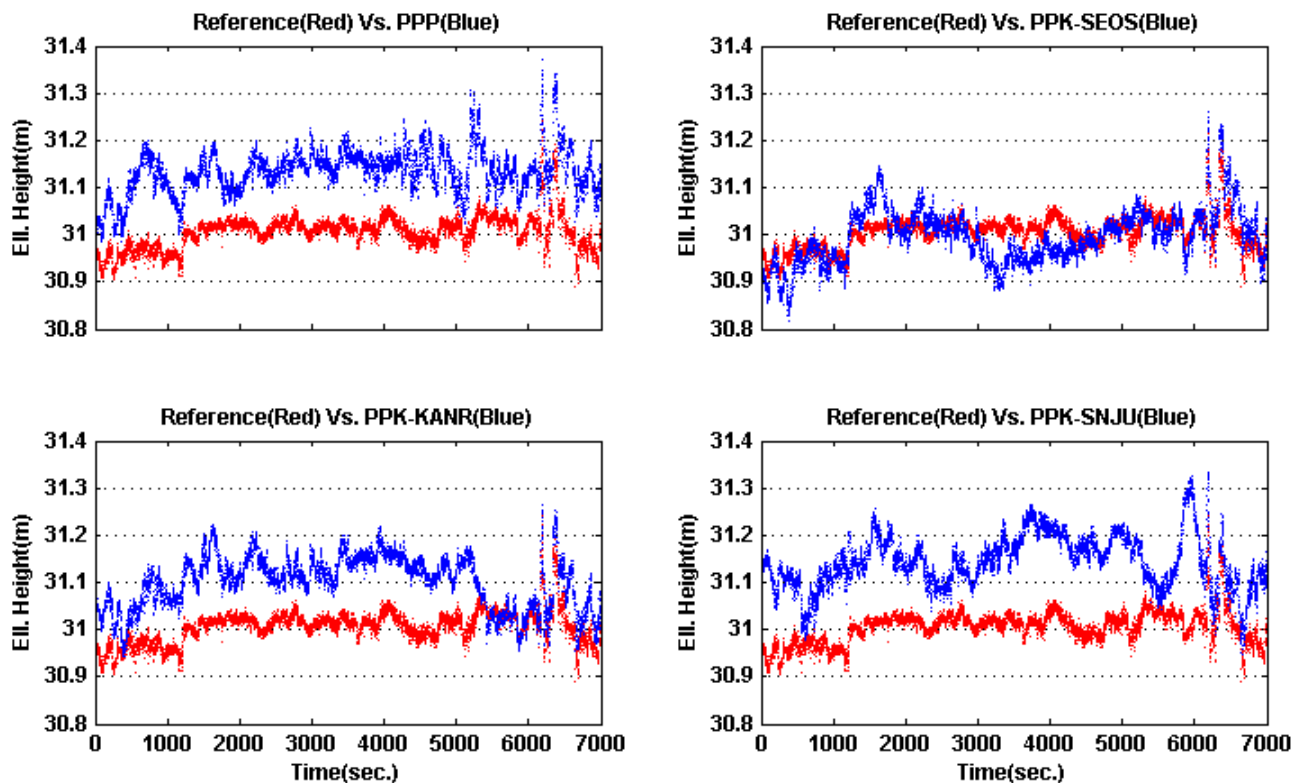


- ✓ The experiment was conducted around West Nakdong River in Busan, Korea.
- ✓ GPS observation was made for approximate 2 hours by 3 rover receivers

# SURVEY VESSEL TEST - EXAMPLE



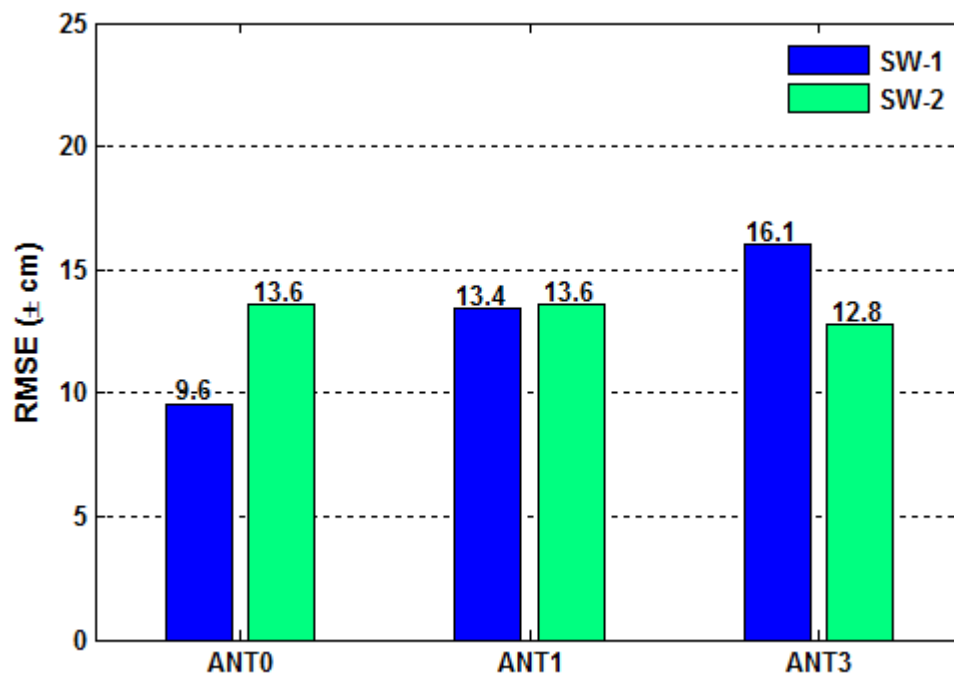
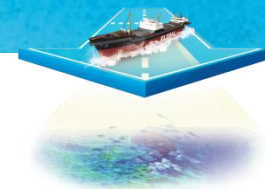
## Comparison with the reference trajectory (example of ANT0)



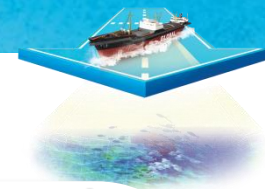
- ✓ Bias is clearly in the results, expect for PPK-SEOS.
- ✓ Considering characteristics of errors in measurement models, it seems to be induced by residual troposphere



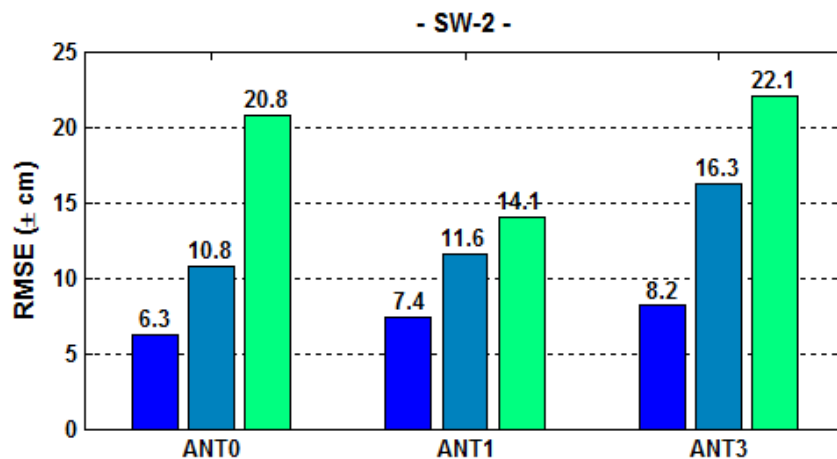
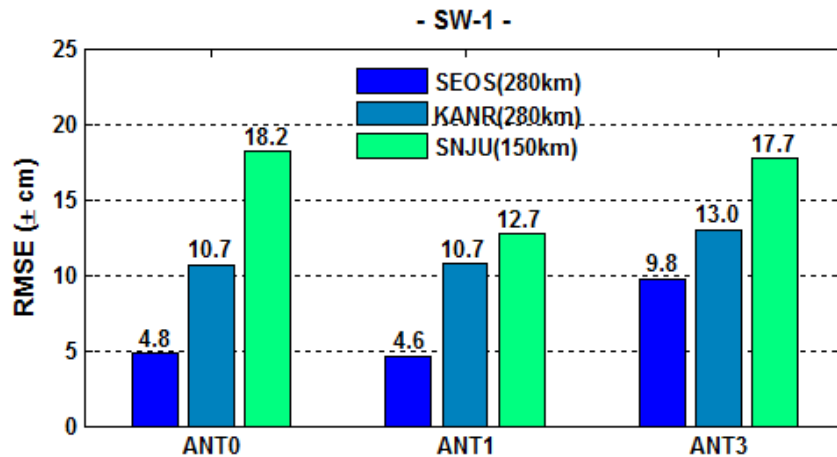
# SURVEY VESSEL TEST - PPP



- ✓ S/W does not much impact into accuracy, but SW-2 provides more stable solutions.
- ✓ GNSS-derived height accuracy by PPP ranges from about  $\pm 10\text{cm}$  to  $15\text{ cm}$ .



# SURVEY VESSEL TEST - PPK



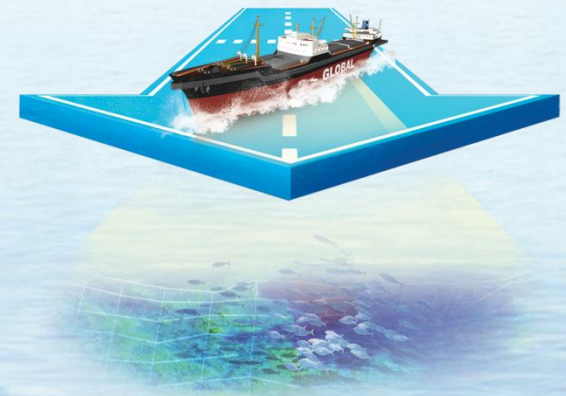
- ✓ Accuracy highly depends on selection of reference station.
- ✓ Baseline distance is not coupled with accuracy.
- ✓ The solutions are less stable than PPP.
- ✓ This might be caused by residual relative troposphere due to different **meteorological condition**.

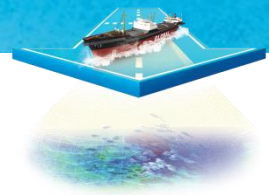
## Some parameter during the test

Site	Temp. (°C)	Humid. (%)
KANR	25 - 26	68 - 75
SEOS	28 - 29	84 - 90
SNJU	31 - 32	59 - 61
Testing Area	27 - 30	79 - 86




IV

# CONCLUDING REMARKS





# CONCLUDING REMARKS

-  Concept and background of ERS has been reviewed with a view to integrating hydrographic and topographic data for costal management.
-  Some potential GNSS data processing schemes have been discussed with emphasis on their features.
-  Results of three experiments were presented to demonstrate achievable accuracy of GNSS height estimation:
  - ***Accuracy of GNSS PPP and medium-range PPK ranges from about 5cm to 20cm.***
  - ***Accuracy of PPP is compatible with that of PPK in height component estimation, but it is dependent on selectin of base station;***
  - ***Two types of software provide almost equivalent results.***
  - ***Further investigation is required to look into impact of residual troposphere to GNSS-estimation.***





Thanks for your attention!  
Any question or comment?



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